

Circular Functions Test 3A

Name: _____

7 8 9 10 11 12



Navigator



Assessment



Student



30 min

Question: 1

If $\sec(x) = 3$ and $\frac{3\pi}{2} \leq x \leq 2\pi$, then $\sin(x)$ is equal to:

- a) $-\frac{\sqrt{3}}{2}$ b) $\frac{\sqrt{3}}{2}$ c) $\frac{1}{3}$ **d) $-\frac{2\sqrt{2}}{3}$** e) $\frac{2\sqrt{2}}{3}$

Question: 2

If $\cot(\alpha) = 1 + \frac{1}{x}$ and $0 \leq \alpha \leq \frac{\pi}{2}$, then $\cos^2(\alpha)$ is equal to:

- a) $\frac{x^2 + 2x + 1}{2x^2 + 2x + 1}$** b) $\frac{x^2}{2x^2 + 2x + 1}$ c) $\frac{x}{\sqrt{2x^2 + 2x + 1}}$ d) $\frac{x + 1}{\sqrt{2x^2 + 2x + 1}}$ e) $\frac{1}{x^2}$

Question: 3

If $\sin(\alpha) = \frac{3}{5}$ and $0 \leq \alpha \leq \frac{\pi}{2}$, then $\sin(2\alpha)$ is equal to:

- a) $\frac{3}{10}$ **b) $\frac{24}{25}$** c) $\frac{12}{25}$ d) $\frac{7}{25}$ e) $\frac{6}{5}$

Question: 4

If $\sin(\alpha) = \frac{3}{5}$ and $\cos(\beta) = \frac{12}{13}$ where $\alpha \in \left[0, \frac{\pi}{2}\right)$ and $\beta \in \left[0, \frac{\pi}{2}\right)$ then $\cos(\alpha - \beta)$ is equal to:

- a) $-\frac{8}{65}$ b) $\frac{16}{65}$ c) $\frac{33}{65}$ **d) $\frac{63}{65}$** e) $\frac{62}{65}$

Question: 5

If $\sec(\alpha) = x$ and $\alpha \in \left(0, \frac{\pi}{2}\right)$ and $\sec(\beta) = x$ where $\beta \in \left(\frac{3\pi}{2}, \frac{5\pi}{2}\right)$ then β in terms of α is:

- a) $2\pi + \alpha$ b) $2\pi - \alpha$ **c) $2\pi \pm \alpha$** d) $\pi + \alpha$ e) $\pi \pm \alpha$

Question: 6

Given $y > x > 0$ then $\tan\left(\sin^{-1}\left(\frac{x}{y}\right)\right)$ is equal to:

- a) $\frac{y}{\sqrt{x^2 - y^2}}$** b) $\frac{x}{\sqrt{y^2 - x^2}}$ c) $\frac{x}{y - x}$ d) $\frac{\sqrt{y^2 - x^2}}{x}$ e) $\frac{\sqrt{y^2 - x^2}}{y}$

Question: 7

Given $0 \leq x \leq 1$ then $\sin\left(\sin^{-1}(x) + \sin^{-1}\left(\sqrt{1-x^2}\right)\right)$ is equal to:

- a) $\frac{\pi}{2}$ b) π c) 0 d) -1 e) 1

Question: 8

The graph of $y = \tan^{-1}\left(\frac{x}{2}\right)$ has asymptotes at:

- a) $y = -2$ and $y = 2$ b) $x = -2$ and $x = 2$
 c) $y = -\frac{\pi}{2}$ and $y = \frac{\pi}{2}$ d) $x = -\frac{\pi}{2}$ and $x = \frac{\pi}{2}$
 e) $y = -\pi$ and $y = \pi$

Question: 9

Given the function defined by the rule: $f(x) = a + b \sin^{-1}(cx)$ where a , b and c are real, non-zero constants, then the maximal domain of $f(x)$ is:

- a) $[-c, c]$ b) $\left[-\frac{a}{b}, \frac{a}{b}\right]$
 c) $\left[\frac{c(a-1)}{b}, \frac{c(1-a)}{b}\right]$ d) $\left[-\frac{1}{c}, \frac{1}{c}\right]$
 e) $\left[-\frac{\pi}{2c}, \frac{\pi}{2c}\right]$

Question: 10

Given the function defined by the rule: $f(x) = a + b \tan^{-1}(c(x-d))$ where a , b , c and d are real positive constants, then the range of $f(x)$ is:

- a) $[a-b, a+b]$ b) $(-\infty, \infty)$
 c) $[a-b\pi, a+b\pi]$ d) $\left(a - \frac{b\pi}{c}, a + \frac{b\pi}{c}\right)$
 e) $\left(a - \frac{b\pi}{2}, a + \frac{b\pi}{2}\right)$